Measuring individual identity information in animal signals: Overview and performance of available identity metrics

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Abstract
1. Identity signals have been studied for over 50 years but, and somewhat remarkably, there is no consensus as to how to quantify individuality in animal signals. While there is a variety of different metrics to quantify individuality, these methods remain un-validated and the relationships between them unclear.
2. We contrasted three univariate and four multivariate identity metrics (and their different computational variants) and evaluated their performance on simulated and empirical datasets.
3. Of the metrics examined, Beecher’s information statistic \(H^*_S\) performed closest to theoretical expectations and requirements for an ideal identity metric. It could be also easily and reliably converted into the commonly used discrimination score (and vice versa). Although Beecher’s information statistic is not entirely independent of study sampling, this problem can be considerably lessened by reducing the number of parameters or by increasing the number of individuals in the analysis.
4. Because it is easily calculated, has superior performance, can be used to quantify identity information in single variable or in a complete signal and because it indicates the number of individuals who can be discriminated given a set of measurements, we recommend that individuality should be quantified using Beecher’s information statistic in future studies. Consistent use of Beecher’s information statistic could enable meaningful comparisons and integration of results across different studies of individual identity signals.

Keywords
acoustic discrimination, acoustic identification, Beecher’s information statistic, discriminant analysis, identity signal, individual recognition, social behaviour, vocal individuality
1 | INTRODUCTION

The fact that individuals differ in consistent ways is both a central attribute of life and one that underlies a number of theoretically important questions such as explaining cooperative behaviour or understanding the evolution of sociality (Bradbury & Vehrencamp, 1998; Crowley et al., 1996; Tibbetts, 2004). Such individuality can also be important in wildlife conservation as well when it is used to help census or monitor individuals based on individually distinctive traits (Blumstein et al., 2011; Terry & McGregor, 2002). And, because, animals may base their decisions on the identity of the individual with whom they interact or respond to (Godard, 1991; Wilkinson, 1984), there may be selection to both produce individually distinctive signals, and selection to discriminate among them (Tibbetts & Dale, 2007; Wiley, 2013).

Quantification of individual identity (individuality) requires the assessment of variation in one or more traits between at least two individuals. For identity signals to function properly, they should maximize the between-individual variation and minimize the within-individual variation (Beecher, 1982, 1989). A variety of identity metrics have proliferated because of recognized biases (e.g., it is more likely to find similar individuals in larger populations and hence, it will be more difficult to discriminate individuals in large populations or studies involving more individuals). These biases make the comparison of results among studies unreliable (Beecher, 1989; Mathevon, Koralek, Weldele, Glickman, & Theunissen, 2010).

Additionally, some existing metrics were considered unsuitable for a particular signal type (Searby & Jouventin, 2004). Nevertheless, new alternatives were not always thoroughly tested and were not shown to be superior to the metrics they attempted to replace. Furthermore, there are methodological problems that result from the calculation of particular identity metrics, and some studies have used different equations to calculate the same identity metric. Thus, somewhat remarkably given its importance, there is no consensus about how to properly measure identity. As a result, researchers have generally avoided quantitative comparisons between studies (Insley, Phillips, & Charrier, 2003). In a few cases, researchers tried to overcome problems with identity metrics in comparative analyses by using exactly the same methods across involved species (Beecher, Medvin, Stoddard, & Loesche, 1986; Lengagne, Lauga, & Jouventin, 1997; Pollard & Blumstein, 2011). Thus, hundreds of isolated studies have been published on individuality in animal signals but because they used different metrics there is limited prospect that we can benefit from the cumulative evidence of these studies. The lack of a commonly used identity metric is a major impediment towards understanding the evolution of identity signalling and indeed, the evolution of individuality.

Here, we review previously developed univariate (quantifying individuality within a single trait) and multivariate metrics (quantifying individuality across multiple traits) that have been used to quantify individual identity information in signals and we test their performance on simulated and empirical datasets. In particular, we examine the following metrics: F-value, Potential of individual coding PIC, Beecher’s information statistic $H_S$, Information capacity $H_M$, and Mutual information MI. We further evaluate the different computational variants found in the literature in case of PIC and $H_S$ (see Table 1 and Supplement 1 for a detailed overview of metrics and their variants).

We compare the performance of metrics to hypothetical ideal identity information metric. The main principle of measuring individual identity in continuous traits is to quantify the ratio of between- and within-individual variation (Beecher, 1982, 1989; Robisson, Aubin, & Bremond, 1993; Searby & Jouventin, 2004). Thus, an ideal individual identity metric should be expressed on a ratio scale with a meaningful zero value, equivalent to the situation when there is no between-individual variation. Further, there is no expected upper limit for individuality. High between-individual variation ratio indicates easy discrimination of individuals.

The datasets for the assessment of individual identity in different species vary in properties such as the number of individuals, the number of samples per individual, the number of variables measured (i.e., number of individualistic traits) and the covariance between the multiple variables measured. Hence, we further propose that an ideal identity metric should be robust or respond predictably to these dataset parameters to allow meaningful comparisons between studies. Therefore, an ideal identity metric: (a) should not be systematically biased by the sampling effort, that is, there should be no systematic effects of number of individuals and number of observations per individual in a study on individuality estimate, and the sampling should ideally only impact on precision of individuality estimate; and (b) in the multivariate case, it should well capture the intrinsic multidimensionality of identity signals. In particular, it should rise with number of meaningful variables because each of the uncorrelated variables can encode another level of individual variation. In addition, it should also decrease with covariance between the variables because increasing covariance between the variables essentially decreases the number of independent variables. For our comparison, we gave the same weight to all criteria because these are very basic requirements and an ideal metric should fulfill all of them. In addition, we will list other potential pros and cons of each metric to provide a comprehensive evaluation of existing metrics.

We also wished to see if each of two commonly used metrics (Beecher’s information statistic $H_S$ and discrimination score DS) could be converted to the other metric. We focused only on $H_S$ and DS metrics. DS has been used in the vast majority of past studies and DS has been found to correlate well with potentially unbiased $H_S$ in a previous study (Beecher, 1989). However, the previous study only tested the relationship between $H_S$ and DS on datasets with equal number of individuals and observations per individual, thus, ignoring the known biases associated with DS. Reliable conversion of DS into potentially unbiased $H_S$ could facilitate comparative analyses of results reported in past and future studies.
<table>
<thead>
<tr>
<th>Metric</th>
<th>Metric variant and equation</th>
<th>Description</th>
<th>Reference</th>
<th>IDmeasurer function</th>
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<tbody>
<tr>
<td><strong>Univariate Metrics</strong></td>
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<tr>
<td>ANOVA F-value (F);</td>
<td>$F = \frac{MS_b}{MS_w}$</td>
<td>$F$ from one-way ANOVA where the individual is treated as independent variable and trait as dependent variable; $MS_b =$ between group mean squares; $MS_w =$ within group mean squares</td>
<td>e.g. Miller (1978)</td>
<td>calcF</td>
</tr>
<tr>
<td>Potential of individual coding (PIC);</td>
<td>$PIC_{beetweentot} = \frac{CV_{beetweentot}}{CV_w}$</td>
<td>$CV_{beetweentot} =$ between-individual coefficient of variation calculated from all data points; $CV_w =$ within-individual coefficient of variation</td>
<td>e.g. Robisson et al. (1993)</td>
<td>calcPICbeetweentot</td>
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<td></td>
<td>$PIC_{betweenmeans} = \frac{CV_{betweenmeans}}{CV_w}$</td>
<td>$CV_{betweenmeans} =$ between-individual coefficient of variation calculated with means from each individual; $CV_w =$ within-individual coefficient of variation</td>
<td>e.g. Lein (2008)</td>
<td>calcPICbetweenmeans</td>
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<tr>
<td>Beecher’s information statistic (H$_S$)</td>
<td>$H_{Sntot} = \log_2 \left( \frac{F + n_{tot} - 1}{n_{tot}} \right)$</td>
<td>$F =$ ANOVA F-value; $n_{tot} =$ total sample size</td>
<td>Possible variant from Beecher (1989)</td>
<td>calcHSntot</td>
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<td>$H_{Sngroups} = \log_2 \left( \frac{F + n_{groups} - 1}{n_{groups}} \right)$</td>
<td>$F =$ ANOVA F-value; $n_{groups} =$ number of groups (individuals)</td>
<td>possible variant from Beecher (1989); e.g. Pollard, Blumstein, &amp; Griffin (2010)</td>
<td>calcHSngroups</td>
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<td>$H_{Snpergroup} = \log_2 \left( \frac{F + n_{pergroup} - 1}{n_{pergroup}} \right)$</td>
<td>$F =$ ANOVA F-value; $n_{pergroup} =$ number of samples in each group (observations per individual)</td>
<td>possible variant from Beecher (1989)</td>
<td>calcHSnpergroup</td>
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<td></td>
<td>$H_{Svarcomp} = \log_2 \frac{\sigma_T}{\sigma_W}$</td>
<td>$\sigma_T =$ total variance in mixed model; $\sigma_W =$ residual variance associated with random factor in mixed model</td>
<td>Beecher (1989); Carter, et al. (2012)</td>
<td>calcHSvarcomp</td>
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<td><strong>Multivariate Metrics</strong></td>
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<tr>
<td>Beecher’s information statistic (H$_S$)</td>
<td>$H_{Snpergroup} = \log_2 \left( \frac{F + n_{pergroup} - 1}{n_{pergroup}} \right)$</td>
<td>$F =$ ANOVA F-value; $n_{pergroup} =$ number of samples in each group (observations per individual); original variables are subjected to PCA to get uncorrelated components and $H_S$ is calculated and summed over each independent component</td>
<td>Beecher (1989)</td>
<td>calcHSnpergroup</td>
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<td>Information capacity (H$_M$)</td>
<td>$H_M = \log_2 \left( \frac{\sum_{i=1}^{n-1} \text{dist}_i}{\text{dist}_w} \right)$</td>
<td>$\text{dist}_i =$ sum of distances of all samples from their centroid; $\text{dist}_w =$ sum of distances of samples within individual to its centroid; $n =$ number of observations; $g =$ number of groups;</td>
<td>Searby and Jouventin (2004)</td>
<td>calcHM</td>
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<td>Discrimination score (DS)</td>
<td>$DS = \frac{C}{N}$</td>
<td>$C =$ samples correctly classified by Discriminant analysis; $N =$ total number of samples</td>
<td>e.g. Hafner et al. (1979)</td>
<td>calcDS</td>
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<tr>
<td>Mutual information (MI)</td>
<td>$MI = \sum_{ij} \log_2 \left( \frac{p(i,j)}{p(i)p(j)} \right)$</td>
<td>$p(i) =$ probability of predicted individual; $p(j) =$ probability of actual individual; $p(i,j) =$ probability of match between predicted and actual individual</td>
<td>Mathevon et al. (2010)</td>
<td>calcMI</td>
</tr>
</tbody>
</table>
2 | MATERIALS AND METHODS

We used R for simulations and statistical analysis (R Core Team, 2012). Functions to calculate identity metrics, associated functions and datasets are available within an IDmeasurer package. This package is available on CRAN (https://cran.r-project.org/web/packages/IDmeasurer/index.html) and GitHub (https://github.com/pygmy83/IDmeasurer).

2.1 | Datasets

2.1.1 | Simulated datasets

Datasets were constructed to mimic typical data on individuality (Figure 1). Parameters of datasets vary among studies. In particular, there are different numbers of individuals, observations (samples) per individual, variables and different covariances among variables. Effect of these parameters was simulated along with individuality within datasets. The level of individual identity in data was modified by changing the ratio of between- and within-individual variance in accordance with theoretical assumptions of individual identity signals and previous studies (Beecher, 1989; Searby & Jouventin, 2004). We developed R scripts involving “rnorm” and MASS package (Venables & Ripley, 2002) “mvrnorm” function to generate the datasets. These functions generate random values with a given standard deviation around pre-specified mean and, in “mvrnorm”, with pre-specified covariance.

We constructed datasets with univariate and multivariate normal distributions with parameters covering a wide range of values, specifically, five values for individuality (id = 0.01, 1, 2.5, 5 and 10), five values for number of observations per individual (o = 4, 8, 12, 16 and 20), eight values for number of individuals (i = 5, 10, 15, 20, 25, 30, 35 and 40). Additionally, for multivariate datasets, five values for covariance among variables (cov = 0, 0.25, 0.5, 0.75 and 1) and five values for number of variables (p = 2, 4, 6, 8 and 10). Thus, 200 and 5,000 unique parameter combinations were possible in case of univariate and multivariate datasets respectively. Individuality (id) represents the ratio of standard deviations between and within individuals (id = $SD_{between} / SD_{within}$; $SD_{between}$ was calculated from means for each individual and $SD_{within}$ was set to be $SD_{between} / id$ (Figure 1). A single covariance (cov) value was used in the variance–covariance matrix to define covariances between all pairs of variables. For univariate datasets, we first generated individual means for a pre-defined number of individuals (normal distribution, “rnorm” function, $M = 1.000$, $SD_{between} = 1$) and then we generated a pre-defined number of random observations “o” around each individual mean (normal distribution, “rnorm” function, mean = individual mean, $SD_{within} = SD_{between} / individuality$ “id”). In the multivariate case, we first created a matrix representing mean individual values of variables for each of the individuals (multivariate normal distribution, “mvrnorm” function, mean for each variable = 0, variance-covariance matrix). Variances on the diagonal of the covariance matrix were set equal to 1 (hence $SD_{between} = 1$) and all covariances between variable pairs were set equal to the pre-defined covariance “cov”. Then, we generated a pre-defined number of random observations “o” around each individual and a variable mean (“rnorm” function, mean = individual mean, $SD_{within} = SD_{between} / individuality$ “id”).

We asked how dataset parameters (i, o, p, cov, id) influenced the value of each identity metric. To explore this, 20 randomization cycles were run for each unique combination of parameter values. For example, in the multivariate case, 20 * 5,000 = 100,000 independent datasets were generated (datasets 1-20: i = 5, o = 4, p = 2, cov = 0, id = 0.01; datasets 21-40: i = 5, o = 4, p = 2, cov = 0, id = 0.01; ...; datasets 99,981-100,000: i = 40, o = 20, p = 10, cov = 1, id = 10). Identity metrics were calculated for each dataset.

2.1.2 | Empirical datasets

While the general performance of identity metrics was evaluated on simulated datasets, empirical datasets were used to evaluate the consistency of DS and HS metrics and reliability of HS and DS conversion on real data. We used six empirical datasets from four different species: little owls Athene noctua (ANmodulation, ANspec) (Linhart & Šálek, 2017), corncrake Crex crex (CCformants, CCspec) (Budka & Osiejuk, 2013), yellow-breasted boubous Laniarius atroflavus

![Figure 1](image_url)

**Figure 1** Illustration of three artificial multivariate datasets that differ only in the individuality used to generate datasets. Settings for the function generating these datasets: $i = 5$, $o = 10$, $p = 2$, $cov = 0$, $id = 0.01$, 3 and 10
deal with normality issues by eliminating problematic variables (e.g. Couchoux & Dabelsteen, 2015), using nonparametric classification methods (e.g. Mielke & Zuberbuehler, 2013), or by relying on robustness of cross-validated DFA and Principle Component Analysis (PCA) towards relaxed assumptions (e.g. Mathevon et al., 2010). We used the last approach. If the assumptions of discriminant analysis that are not met the results should be less stable when using different sampling and hence our results should be viewed as conservative.

2.2 Statistical analysis

The relationship between a given identity metric and each of the parameters was assessed graphically by plotting the mean value and the 95% confidence intervals of an identity metric against all of the modelled data parameters separately. We then used a one-way ANOVA to test whether an identity metric was constant across all levels of a parameter. One-way ANOVA along with graphical evaluation of relationships between metrics and model parameters was preferred over multivariate regression because it simply, but adequately, addresses our main question (i.e. does the metric change in response to model parameter?) without the need to specify and compare many different multivariate regression models. If we found significant differences, we followed up these with post-hoc Tukey tests to identify which parameter levels differed. Due to the large number of comparisons, we only reported comparisons of neighbouring parameter levels. We used linear and nonparametric loess regression to convert HS to DS and vice versa.
Loess regression identifies a function that best describes complex data by fitting simple models to sequential subsets of data. Its main advantage is that it does not require specifications of the function and, hence, it is suitable for modelling of complex relationships. Loess regression included the number of individuals and the number of observations per individual as additional predictors. We used Spearman correlation coefficients to quantify between-metric consistency of ranking individuality in datasets. Pearson correlations were used to assess consistency within identity metrics in full and partial datasets. We then used Friedman tests, followed by a series of Wilcoxon tests (for post-hoc comparison of differences between levels), to compare correlation coefficients obtained for each pair of the metrics.

3 | RESULTS

The comparison of available univariate and multivariate metrics to an ideal metric is shown in Table 2.

3.1 | Univariate metrics

All explored univariate metrics increased with increasing individuality in the data. However, only $\text{PIC}_{\text{between}}$, $\text{PIC}_{\text{betweenmeans}}$, $\text{H}_{\text{Snpergroup}}$ and $\text{HS}_{\text{varcomp}}$ estimates were independent of the number of observations and the number of individuals used to calculate the metric (Figure 3). These general patterns were qualitatively identical when all simulated data were pooled or if only one of the parameters (number of observations, number of individuals, individuality) was changed at a time and the others were kept constant at the middle value (see Supplement 3 for detailed results including ANOVA tests).

All four sampling-independent metrics ($\text{PIC}_{\text{between}}$, $\text{PIC}_{\text{betweenmeans}}$, $\text{H}_{\text{Snpergroup}}$ and $\text{HS}_{\text{varcomp}}$) were highly correlated (Spearman correlation, all $r > 0.99$), $\text{H}_{\text{Snpergroup}}$ and $\text{HS}_{\text{varcomp}}$ correctly converged to 0 in the case when individuality was set to be negligible (id = 0.01), while $\text{PIC}_{\text{between}}$ and $\text{PIC}_{\text{betweenmeans}}$ converged to higher values (1.01 and 0.32 respectively). $\text{PIC}_{\text{between}}$ reflects the number of potential individual signatures within a population in the same way as $2^{\text{nd}}$ does (Beecher, 1989), and, both, $\text{PIC}_{\text{between}}$ and $\text{PIC}_{\text{betweenmeans}}$ reflect the ratio of between- to within-individual variation. Hence, convergence of $\text{PIC}_{\text{between}}$ to 1 could be also seen as desirable quality and meaningful value for a signal with no individuality. $\text{HS}_{\text{varcomp}}$ was equal to $2^*\text{H}_{\text{Snpergroup}}$ (see Supplement 4 for details). We further considered only the $\text{H}_{\text{Snpergroup}}$ variant in multivariate analyses.

3.2 | Multivariate metrics

The performance of multivariate identity metrics is illustrated in Figure 4. All metrics increased with increasing individuality. DS, $H_S$ and MI increased with increasing number of variables available and decreased with increasing covariance between variables. Only $H_M$ did not change in response to increasing the number of individuals. $H_S$ and $H_M$ did not change in response to increasing the number of observations per individual. These general patterns were qualitatively identical when all simulated data were pooled or if only one dataset parameter was changed at a time and others were kept constant at the middle value (see Supplement 5 for detailed results including ANOVA tests).

Despite the different response of metrics to some of the simulated parameters, there was still moderate to high agreement among metrics about identity content in the data (Spearman correlations, mean $r \pm SD = 0.82 \pm 0.07$; minimum $r = 0.71$ for correlation between DS and MI; maximum $r = 0.95$ for correlation between DS and $H_J$). $H_J$ had the greatest correlations with other metrics (average $R = 0.88$). We found no advantage to using $H_M$ over $H_S$ as previously suggested. Instead, $H_M$ was equal to $H_S$ per variable ($H_M = H_S/p$) in data with zero covariance between variables. (Supplement 6).

Thus, our simulations show that $H_J$ matched the characteristics of the ideal metric in 6/7 cases, followed by $H_M$ (5/7), DS (4/7) and MI (both 3/7) (Table 1).

3.3 | Potential for removing bias in $H_S$

We observed no significant association between $H_S$ and the number of individuals in the univariate case, so we investigated the origin of the sampling bias in the multivariate case. This bias was only present when data were subjected to PCA. However, PCA is required to create uncorrelated components for $H_S$ calculation.

It is possible that the more variables measured, the more individuals need to be sampled in order to reduce this bias. We therefore fixed the number of variables to 5, 10 and 20 ($p = 5, 10, 20$) and varied the ratio of the number of individuals to the number of variables “i to p ratio” from 0.5 to 5 (“i to p ratio” = 0.5, 1, 1.5, 2, 3, 5) by using different numbers of individuals in our simulations ($i = 3, 5, 8, 10, 15, 20, 25, 30, 40, 50, 60, 100$ depending on number of variables and “i to p ratio”). The number of observations per individual was set to 10. Individuality and covariance were both chosen randomly in each iteration from pre-defined intervals used in the earlier simulations (covariance range = [0, 0.25, 0.5, 0.75, 1]; individuality range = [0.01, 1, 2.5, 5, 10]). We used 100 iterations for each “i to p ratio”. $H_S$ did not rise significantly after the number of individuals reached at least the number of parameters (One-way ANOVA $F_{5,1794} = 7.68$, $p < 0.001$; no significant differences between levels if “i to p” $\geq 1$, all $p > 0.132$) (Figure 5).

3.4 | Converting DS to $H_S$ and vice versa

We used simple linear regression and non-parametric loess regression to estimate $H_S$ based on DS and vice versa. There was a previously suggested linear relationship that had a limit of $H_S = 8$ where the DS values were 100% correct discrimination (Beecher, 1989). Because the $H_S$ values in our original simulated datasets far exceeded 8, we generated a new set of simulated datasets with individuality ranging between 0.1 and 2 (id = 0.1, 0.25, 0.5, 0.75, 1, 1.33, 2.5, 5, 10).
**TABLE 2** The comparison of available univariate and multivariate metrics to a hypothetical ideal metric and summary of their pros and cons. We summed the number of matches (points) to compare different metrics to the ideal metric.

<table>
<thead>
<tr>
<th></th>
<th>Zero</th>
<th>Limit</th>
<th>id</th>
<th>cov</th>
<th>p</th>
<th>o</th>
<th>i</th>
<th>Points</th>
<th>Pros</th>
<th>Cons</th>
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<tbody>
<tr>
<td><strong>Univariate metrics</strong></td>
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<tr>
<td>Ideal</td>
<td>y</td>
<td>n</td>
<td>+</td>
<td>ns</td>
<td>ns</td>
<td>5</td>
<td>5</td>
<td>5/5</td>
<td></td>
<td>Sample dependent</td>
</tr>
<tr>
<td>F</td>
<td>y</td>
<td>n</td>
<td>+</td>
<td>+</td>
<td>ns</td>
<td>4</td>
<td>5</td>
<td>4/5</td>
<td>Intuitive and straightforward calculation; allows separate assessment of within- and between-individual variation</td>
<td>Not meaningful for variables with positive and negative values; cannot be summed or averaged over different variables = univariate only</td>
</tr>
<tr>
<td>PIC&lt;sub&gt;between&lt;/sub&gt; &lt;sub&gt;tot&lt;/sub&gt;</td>
<td>y</td>
<td>n</td>
<td>+</td>
<td>ns</td>
<td>ns</td>
<td>5</td>
<td>5</td>
<td>5/5</td>
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<tr>
<td>PIC&lt;sub&gt;between&lt;/sub&gt; &lt;sub&gt;means&lt;/sub&gt;</td>
<td>n</td>
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<td>ns</td>
<td>ns</td>
<td>4</td>
<td>5</td>
<td>4/5</td>
<td></td>
<td>Converges to non-meaningful value for no individuality in data</td>
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<tr>
<td>H&lt;sub&gt;s&lt;/sub&gt; &lt;sub&gt;split&lt;/sub&gt;</td>
<td>y</td>
<td>n</td>
<td>+</td>
<td>ns</td>
<td>-</td>
<td>4</td>
<td>5</td>
<td>4/5</td>
<td>Sample dependent; incorrect HS variant</td>
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<tr>
<td>H&lt;sub&gt;s&lt;/sub&gt; &lt;sub&gt;pergroup&lt;/sub&gt;</td>
<td>y</td>
<td>n</td>
<td>+</td>
<td>ns</td>
<td>ns</td>
<td>5</td>
<td>5</td>
<td>5/5</td>
<td>Standard variant of HS; univariate and multivariate</td>
<td>Sample dependent; incorrect HS variant</td>
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<tr>
<td>H&lt;sub&gt;s&lt;/sub&gt; &lt;sub&gt;ngroups&lt;/sub&gt;</td>
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<td>H&lt;sub&gt;s&lt;/sub&gt; &lt;sub&gt;varcomp&lt;/sub&gt;</td>
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<td>+</td>
<td>ns</td>
<td>ns</td>
<td>5</td>
<td>5</td>
<td>5/5</td>
<td>Allows including various covariates in mixed models</td>
<td>Values twice as big as in case of standard HS&lt;sub&gt;pergroup&lt;/sub&gt;</td>
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<td><strong>Multivariate metrics</strong></td>
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<td>Ideal</td>
<td>y</td>
<td>n</td>
<td>+</td>
<td>-</td>
<td>+</td>
<td>3</td>
<td>7</td>
<td>7/7</td>
<td>Population and individual metric; the most commonly used metric</td>
<td>Sample dependent; not suitable for high individuality signals because values are limited from the top</td>
</tr>
<tr>
<td>DS</td>
<td>n</td>
<td>y</td>
<td>+</td>
<td>-</td>
<td>+</td>
<td>3</td>
<td>7</td>
<td>3/7</td>
<td></td>
<td></td>
</tr>
<tr>
<td>H&lt;sub&gt;s&lt;/sub&gt;</td>
<td>y</td>
<td>n</td>
<td>+</td>
<td>-</td>
<td>+</td>
<td>ns</td>
<td>6</td>
<td>7/7</td>
<td>Univariate and multivariate; partial sample dependence is introduced by PCA but can be to large extent eliminated; biologically meaningful - provides number of unique individual signatures within population; good theoretical framework for both discrete and continuous individuality traits</td>
<td>Partially sample dependent</td>
</tr>
<tr>
<td>H&lt;sub&gt;M&lt;/sub&gt;</td>
<td>y</td>
<td>n</td>
<td>+</td>
<td>ns</td>
<td>ns</td>
<td>ns</td>
<td>5</td>
<td>7/7</td>
<td>Sample independent; various types of similarity metrics can be potentially used (euclidean distances, Jaccard similarity, string edit distance, dynamic time warping, etc.)</td>
<td>Number of independent variables needs to be known to calculate total identity information</td>
</tr>
<tr>
<td>MI</td>
<td>n</td>
<td>y</td>
<td>+</td>
<td>-</td>
<td>+</td>
<td>-</td>
<td>3</td>
<td>7/7</td>
<td>Could be applied with various classification methods</td>
<td>Sample dependent; not suitable for high individuality signals because values are limited from the top</td>
</tr>
</tbody>
</table>

Abbreviations: zero, metric has a meaningful zero; limit, metric is limited from the top by an asymptote; id, change in response to increasing identity information in data; cov, response to increasing covariance between variables; p, response to increasing number of variables; o, response to increasing number of observations per individual; l, response to increasing number of individuals; y, yes; n, no; +, increase; -, decrease; ns, not significant, does not change with a parameter.
FIGURE 3  Variation in univariate identity metrics in response to simulated dataset parameters: individuality, number of observations per individual and number of individuals. Means and 95% confidence intervals are shown. Graphs were plotted using all simulated univariate data pooled together. For the graphs with only a single parameter changing at a time see Supplement 3.
1.66, 2), covariance set to zero (cov = 0), number of iterations was reduced to 10 (it = 10), and other parameters were set as in previous models (p = 2, 4, 6, 8, 10; i = 5, 10, 15, 20, 25, 30, 35, 40; o = 4, 8, 12, 16, 20). These settings led to $H_S$ values up to about 13 for data used for model building, and $H_S$ values up to about 14 in the case of data used for model testing. These values are much closer to 8 and also much closer to $H_S$ values reported from nature.

Loess models took into account the number of observations per individual and the number of individuals. We compared the loess conversion and linear conversion models of DS and $H_S$. In general, loess estimates were closer to the ideal prediction (intercept = 0, beta = 1) and the loess model reduced the error of both DS and $H_S$ estimates to about a half compared to linear estimates (Figure 6). Both $H_S$ estimates were underestimated for high values of $H_S$. The ceiling value is clearly apparent for linear estimates of $H_S$. It is still visible in the case of loess estimates but loess predictions remain reasonably good up to about $H_S = 10$.

### 3.5 Correlations between calculated and estimated metrics

We were further interested in how $H_{\text{est}}$ and $DS_{\text{est}}$ might represent $H_S$ and DS of a particular sample of individuals or $H_{\text{full}}$ and $DS_{\text{full}}$ of the whole population. For this purpose, we first generated 50 full datasets with different identity levels representing 50 hypothetical populations of different species. Each dataset comprised 40 individuals, 20 calls per individual and 10 parameters. For these datasets, individuality was set randomly ranging between 0.2 and 2 (0.1 increments), and the covariance was set randomly ranging between 0.2 and 0.8 (0.1 increments). These settings generated datasets with $H_{\text{full}}$ values that ranged from 0.22 to 9.89 ($M \pm SD: 4.72 \pm 2.95$). Then, we repeatedly subsampled full datasets to get partial datasets which simulated different sampling of the population. We subsampled 5–40 individuals and 4–20 calls per individual per dataset in...
Each of total 20 iterations. We also repeatedly resampled our empirical datasets. We resampled 5–33 individuals and 4–10 calls per individual per dataset in each of total 20 iterations. The number of parameters was not randomized—we always kept the original number of variables.

In simulated datasets, \( H_5 \) and \( H_{\text{est}} \) were correlated almost perfectly with each other and with \( H_{\text{full}} \) (all average Pearson \( r > 0.97 \)). There was no difference among the correlation coefficients from correlations between \( H_{\text{full}} \), \( H_5 \) and \( H_{\text{est}} \) (Friedman Chi Square = 3.6, \( p = 0.165 \)). In empirical datasets, \( H_5 \) calculated on partial datasets still reflected the \( H_{\text{full}} \) almost perfectly (average Pearson \( r = 0.99 \)). While \( H_{\text{est}} \) reflected \( H_5 \) of partial dataset (average Pearson \( r = 0.90 \)) and \( H_{\text{full}} \) (average Pearson \( r = 0.88 \)) slightly worse, it remained a reasonable fit. However, \( H_{\text{est}} \) did not reflect \( H_{\text{full}} \) as precisely as it did \( H_5 \) (Friedman Chi Square = 33.6, \( p < 0.001 \), post-hoc test: \( H_5 - H_{\text{full}} \) vs. \( H_{\text{est}} - H_{\text{full}} \), \( p < 0.001 \)).

\( DS \) in simulated datasets was almost perfectly correlated with \( DS_{\text{est}} \) (average Pearson \( r = 0.99 \)). Although the relationship between \( DS \) in full datasets (\( DS_{\text{full}} \)) and \( DS \) and \( DS_{\text{est}} \) was significantly worse (Friedman Chi Square = 40.0, \( p < 0.001 \); both post-hoc tests: \( p < 0.005 \)), these associations remained strong (\( DS_{\text{full}} \) and \( DS \): average Pearson \( r = 0.95 \); \( DS_{\text{full}} \) and \( DS_{\text{est}} \): average Pearson \( r = 0.96 \)). In empirical datasets, the correlation between \( DS \) and \( DS_{\text{est}} \) was lower than in case of artificial datasets (average Pearson \( r = 0.91 \)). \( DS \) and \( DS_{\text{est}} \) of partial datasets had comparable correlations to \( DS_{\text{full}} \) (\( DS_{\text{full}} \) and \( DS \): average Pearson \( r = 0.88 \); \( DS_{\text{full}} \) and \( DS_{\text{est}} \): average Pearson \( r = 0.86 \)). Thus, the performance of \( DS \) and \( DS_{\text{est}} \) to reflect each other or \( DS_{\text{full}} \) did not differ (Friedman Chi Square = 0.9, \( p = 0.638 \)).

4 DISCUSSION

We provided an overview of the metrics used to quantify individual identity in animal signals in order to identify the best method for reporting individuality in animal signals. Biases associated with some of the commonly used metrics, and the use of different metrics across studies, make it difficult to compare results and integrate the accumulated knowledge from the numerous published studies on individual identity in animal signals.
We show that the assessment of individual identity is relatively straightforward when considering a single trait (univariate case). Both PIC (\(\text{PIC}_{\text{between}}\)) and \(\text{H}_S\) (\(\text{H}_S\)) were previously found to correlate well with DS (Beecher, 1989; Searby & Jouventin, 2004). We extend previous findings for \(\text{H}_S\) (Beecher, 1989) to situations with unequal sampling and we show it is possible to convert between \(\text{H}_S\) and DS with an acceptable amount of error even when datasets differ in the number of individuals and observations per individual, and have important issues associated with multivariate normality (Supplement 2). Discriminant analysis (DA) and Principal component analysis (PCA) used for DS and \(\text{H}_S\) calculations both assume multivariate normality for optimal results. While using these methods with non-normal data cannot be, in general, recommended, relatively high correlations between our metrics in empirical datasets suggest that DA and PCA scores were quite robust to these normality issues. Discrimination and dimensionality reduction analytical techniques that are able to handle normal and non-normal data definitely need to be considered in future individual identity studies.

4.2 | Future individual identity metrics

We hope that our study will stimulate further discussions about how individual identity should be properly measured. Although we suggest that \(\text{H}_S\) should be generally used to quantify individuality, different metrics or more complex approaches might be required for particular interesting questions. For example, \(\text{H}_S\) can only provide a population estimate of individual identity. Researchers might be interested in whether distinctiveness of individuals increases during ontogeny (Syrová et al., 2017). In this case, discrimination scores can be reported for each individual, thus making statistical evaluation possible. Furthermore, separate assessments of within- and between-individual variations when calculating PIC might be useful to test hypotheses about which of the two has been selected for. Within-individual variation could be reduced by, for example, ritualized behaviour while between-individual variation could be increased through, for example, morphological variation in structures producing or carrying the signal (e.g. Sheehan & Nachman, 2014). The dimensionality of identity signals might be an important factor for recognition processes (Trunk, 1979) and evolution could favour low dimensional signals. Paralleling the distribution of individuals in space (territoriality, living in colonies), individual signatures within a population, too, could have random, clumped, or regular distributions depending on the mechanisms behind individual distinctiveness and the degree of plasticity of identity signals.

We evaluated the efficacy of all metrics within the acoustic modality only. It is increasingly recognized that signals employ multiple modalities (Partan, 2013; Partan & Marler, 1999). All of the identity metrics discussed here could be, in principal, used in visual or chemical domains as well. \(\text{H}_S\) has an advantage that it could be used both for discrete traits, such as colour variants, presence of particular alleles or chemicals, and for continuous traits such as size of visual patterns, duration of calls, etc. (Beecher, 1982, 1989). However, identity
information outside the acoustic domain has been rarely quantified and meaningful comparison of individual identity across modalities remains a challenge for the future.

It is likely that automatic data collection and analysis techniques will be increasingly applied for various recognition tasks, including individual recognition (Elie & Theunissen, 2018; Stowell, Petrusková, Šálek, & Linhart, 2019). While these methods will allow studying individual identity signalling on unprecedented scales and sample sizes, the resulting classification accuracy scores will be analogous to the discrimination score, with similar positives and drawbacks. However, many different feature sets, pre-defined or automatically derived from data, as well as many different classification methods could be combined to test for the robustness of identity signals and/or to mimic and test for different alternatives of possible real recognition processes (Elie & Theunissen, 2018).

5 | CONCLUSION

We suggest that, at the current state of knowledge and methodology development, Hs should be generally reported as the “golden standard” individual identity metric to allow the best comparison of individuality in signals across different studies. Given that Hs may not be sufficient in all cases, we encourage further research to develop new metrics to quantify identity information in signals. However, new metrics should always be appropriately assessed and their performance directly compared to the best existing metrics. We provide datasets and scripts that should help to assess individual identity information in animal signals and benchmark the future metrics.

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AUTHORS’ CONTRIBUTIONS

P.L. and D.T.B. conceived the ideas, designed methodology and led the writing of the manuscript; P.L., T.O., M.B., M.Šá., M.Śp., M.S. and R.P. collected the data; P.L. analysed the data; All the authors contributed critically to the drafts and gave final approval for publication.

DATA ACCESSIBILITY STATEMENT

Data and code used for this article are available within IDmeasurer package currently available on CRAN (https://cran.r-project.org/web/packages/IDmeasurer/index.html) and GitHub (https://github.com/pymgy83/IDmeasurer).

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